## ICSE - Class X Mathematics - M.L. Agarwal Solution

## Chapter 3 : Shares and Dividends

## Exercise 3

1. Find the dividends received on 60 shares of ₹ 20 each if $9 \%$ dividend is declared.

Solution:
Given value of shares = ₹. 20
Therefore the value of 60 shares $=₹ .20 \times 60$
= ₹. 1200
Given that rate of dividend $=9 \%$
Therefore total dividend $=$ ₹. $1200 \times 9 \%$
$=1200 \times(9 / 100)$
= ₹ 108
2. A company declares 8 percent dividend to the share holde₹. If a man receives a ₹. 2840 as his dividend, find the nominal value of his shares.

## Solution:

Given that rate of dividend $=8 \%$
Also given that amount of dividend $=₹ .2840$
Therefore nominal value of shares $=(2840 \times 100) / 8$
= ₹. 35500
3. A man buys 200 ten-rupee shares at $₹ .12 .50$ each and receives a dividend of $8 \%$. Find the amount invested by him and the dividend received by him in cash.

## Solution:

Given face value of shares = ₹. 10
Number of shares $=200$

Therefore face value of 200 shares $=10 \times 200$
= ₹. 2000
Now, amount invested for the purchase of 200 shares at the rate of ₹. 12.50 each
$=12.50 \times 200$
$=₹ 2500$
Given that rate of dividend $=8 \%$
Therefore total amount of dividend $=(2000 \times 8) / 100$
= ₹. 160
4. Find the market price of $5 \%$ ₹ 100 share when a pe₹on gets a dividend of ₹ 65 by investing ₹. 1430.

## Solution:

Given amount of dividend $=₹ 65$
Also given that rate of dividend $=5 \%$
Therefore total face value $=(65 \times 100) / 5$
= ₹ 1300
If face value is ₹. 1300, then market value $=₹ .140$
If face value is ₹. 100, then market value $=(1430 \times 100) / 1300$
= ₹ 110
5. Salman buys 50 shares of face value ₹ 100 available at ₹ 132 .
(i) what is his investment?
(ii) If the dividend is $7.5 \%$ p.a., what will be his annual income?
(iii) If he wants to increase his annual income by ₹ 150 , how many extra shares should he buy?

## Solution:

Given face value $=₹ 100$
(i) Given that market value $=₹ 132$

And number of shares $=50$
Therefore investment $=$ number of shares $\times$ market value
$=50 \times 132$
= ₹ 6600
(ii) We have income per share $=7.5 \%$ of face value
$=(75 / 10 \times 100) \times 100$
= ₹. 7.5
Therefore annual income $=7.5 \times 50$
= ₹ 375
(iii) Therefore new annual income $=375+150=₹ 525$

Therefore number of shares $=525 / 7.5=70$
Therefore, number of extra share to be increased $=70-50$
$=20$
6. A lady holds 1800 , ₹. 100 shares of a company that pays $15 \%$ dividend annually. Calculate her annual dividend. If she had bought these shares at 40\% premium, what percentage return does she get on her investment? Give your answer to the nearest integer.

## Solution:

Given total number of shares $=1800$
Nominal value of each share $=₹ 100$
And rate o dividend $=15 \%$
Total face value of 1800 shares $=100 \times 1800$
= ₹. 180000
Therefore total dividend $=180000 \times 15 / 100$
$=₹ 2700$
Therefore market value of each share $=100+40=₹ .140$
Now the total investment $=140 \times 1800$
= ₹. 252000
Therefore percentage on his return
$=(27000 \times 100) / 252000$
$=10.7 \%$
In intege₹ 11\%
7. What sum should a pe₹on invest in ₹ 25 shares, selling at ₹ 36 , obtain an income of ₹ 720 , if the dividend declared is $12 \%$ ? Also find the percentage return on his income.

## Solution:

Given nominal value of each share $=₹ .25$
Market value of each share $=₹ .36$
Total income = ₹ 720
Rate of dividend $=12 \%$
Therefore total nominal value $=(100 \times 720) / 12$
= ₹ 6000
Number of shares $=6000 / 25$
$=240$
Total investment $=240 \times 36$
= ₹ 8640
Now, percentage return $=(720 \times 100) / 8640$
= 8.3\%
8. Ashok invests ₹ 26400 on $12 \%$ ₹ 25 shares of a company. If he receives a dividend of ₹ 2475 , find:
(i) The number of shares he bought.
(ii) The market value of each share.

Solution:
Given investment = ₹ 26400
Face value of the each share $=₹ 25$
Rate of dividend $=12 \%$
Total dividend = ₹ 2475
We know that, dividend earned $=$ market price of share $\times$ number of shares $\times \mathrm{r} / 100$
(i) Therefore number of shares $=(2475 / 12) \times(100 / 25)$
= 825 shares
(ii) Market value of each share $=(26400 / 825)$
= ₹ 32
9. A man invests $\square 4500$ in shares of a company which is paying $7.5 \%$ dividend. If 100 shares are available at a discount of 10\%, find
(i) the number of shares he purchases.
(ii) his annual income.

## Solution:

Given,
Investment $=\square 4500$
Face value of each share $=\square 100$
Discount $=10 \%$ and rate of dividend $=7.5 \%$
The market price of each share $=\square(100-25)=\square 75$
(i) The number of shares he purchases $=4500 / 75=60$
(ii) Dividend $=\square 7.5 \%$ of ( $60 \times 100$ )
$=\square 450$
Hence, his annual income will be $\square 450$.
10. Amit kumar invests ₹ 36000 in buying ₹ 100 shares at ₹ 20 premium. The dividend is $15 \%$ per annum. Find:
(i) The number of shares he buys
(ii) His yearly dividend
(iii) The percentage return on his investment.

Solution:
Given investment $=₹ 36000$
Face value = ₹ 100
Premium $=₹ 20$ and dividend $=15 \%$
(i) Number of shares $=36000 / 120$
$=300$
(ii) Dividend $=15 \%$ Of $(100 \times 300)$
$=₹ 4500$
(iii) Percentage of return $=(4500 / 36000) \times 100$
$=450 / 36$
= $12.5 \%$
11. Mr. Tiwari invested ₹ 29040 in $15 \%$ ₹ 100 shares at a premium of $20 \%$. Calculate:
(i) The number of shares bought by Mr. Tiwari
(ii) Mr. Tiwari's income from the investment
(iii) The percentage return on hid investment.

## Solution:

(i) Market value of one share $=[(200 / 100) \times 100]+100$
= ₹ 120
Number of shares = investment/ market value of one share
= 29040/120
= ₹ 242
(ii) Therefore income from investment $=242 \times 15$
= ₹ 3630
(iii) Percentage return on his investment $=($ dividend/ market value) $\times 100$
$=(15 / 120) \times 100$
= $12.5 \%$
12. A man buys shares at the par value of ₹ 10 yielding $8 \%$ dividend at the end of a year. Find the number of shares bought if he receives a dividend of ₹ 300 .

## Solution:

Given face value of each share $=₹ 10$
Rate of dividend $=8 \%$ per annum
Total dividend = ₹ 300
Therefore total face value of shares $=(300 \times 100) / 8$
= ₹ 3750
Number of shares $=3750 / 10$
$=375$
13. A man invests ₹ 8800 on buying shares of face value of rupees hundred each at a premium of $10 \%$. If he earns ₹ 1200 at the end of year as dividend, find:
(i) The number of shares he has in this company
(ii) The dividend percentage per share.

## Solution:

Given investment = ₹ 8800
Face value of each share = ₹ 100
Market value of each share $=100+10=₹ 110$
Total income = ₹ 1200
Therefore total face value $=(8800 \times 100) / 110$
= ₹ 8000
(i) Number of shares $=8000 / 100$
$=80$
(ii) Rate of dividend $=(1200 \times 100) / 8000$
= $15 \%$
14. A man invested ₹ 45000 in $15 \%$ ₹ 100 shares quoted at ₹ 125 . When the market value of these shares rose to ₹ 140 , he sold some shares, just enough to raise ₹ 8400 . Calculate:
(i) The number of shares he still holds.
(ii) The dividend due to him on these shares.

## Solution:

Given investment on shares $=₹ 45000$
Face value of each share = ₹ 125
Therefore total number of shares $=45000 / 125$
$=360$ shares
Income from sold shares $=$ ₹ 8400
Therefore number of shares sold = income from shares/ number of shares sold
$=8400 / 140$
$=60$
(i) Number of shares he still holds $=300$
(ii) Market value of 300 shares $=300 \times 140$
= ₹ 42000
Face value of 300 shares $=300 \times 125$
= ₹ 37500
Difference $=$ Market value - face value
= 42000-37500
= ₹ 4500
15. Ajay owns 560 shares of a company. The face value of each share is ₹ 25 . The company declares a dividend $0 f 9 \%$. Calculate
(i) The dividend that Ajay will get
(ii) The rate of interest, on his investment if Ajay has paid ₹. 30 for each share.

## Solution:

Given number of shares $=560$
Face value of each share $=₹ 25$
Rate of dividend $=9 \%$ per annum
Total face value of 560 shares $=25 \times 560$
= ₹ 14000
(i) Amount of dividend $=14000 \times(9 / 100)$
= ₹ 1260
(ii) Market value of each share $=₹ 30$

Total investment $=30 \times 560$
= ₹ 16800
Therefore percentage of interest on his investment $=(1200 \times 100) / 16800$

$$
=7.5 \%
$$

16. A company with 10000 shares of nominal value of ₹ 100 declares an annual dividend of $8 \%$ to the share holde₹.
(i) Calculate the total amount of dividend paid by the company
(ii) Ramesh bought 90 shares of company at ₹ 150 per share.

Calculate the dividend he received and the percentage return on his investment.

## Solution:

Given number of shares $=10000$
Nominal value of each share $=₹ 100$
Rate of annual dividend $=8 \%$
Total face value of 10000 shares $=100 \times 10000$
= ₹ 1000000
Dividend $=(1000000 \times 8) / 100$
= ₹ 80000
(ii) Number of shares $=90$

Face value of each share $=₹ 150$
Total face value of 90 shares $=100 \times 90$
= ₹ 9000
Therefore amount of dividend $=(9000 \times 8) / 100$
= ₹ 720
Market value of 90 shares $=90 \times 159$
= ₹ 13500
Therefore rate of interest $=(720 \times 100) /(13500 \times 1)$
$=16 / 3$
= 5.3 \%
17. A company with 4000 shares of nominal value of $₹ .110$ declares annual dividend of $15 \%$. Calculate :
(i) the total amount of dividend paid by the company,
(ii) the annual income of Shah Rukh who holds 88 shares in the company,
(iii) if he received only $10 \%$ on his investment, find the price Shah Rukh paid for each share. (2008)

## Solution:

Number of shares $=4000$
Nominal (face) value of each share $=₹ .110$
Total face value of 4000 shares $=₹ .110$
x 4000
$=₹, 440000$
Rate of annual dividend $=15 \%$
(i) Amount of dividend $=(440000 \times 15) / 100$
= ₹ 66000
(ii) Number of shares, Shah Rukh has $=88$

Face value of 88 shares $=88 \times 110$
= ₹ 9680
Annual dividend $=(9680 \times 15) / 100$
= ₹ 1452
(iii) Rate of annual income on his investment $=10 \%$

His investment $=(1452 \times 100) / 10$
= ₹ 14520
Market value of each share $=14520 / 88$
= ₹ 165
18. By investing ₹. 7500 in a company paying 10 percent dividend, an income of $₹ .500$ is received. What price is paid for each ₹. 100 share.

## Solution:

Given investment $=₹ 7500$
Rate of dividend $=10 \%$,
Total income = ₹. 500.
Face value of each share $=₹ 100$
Total face value $=(100 \times 500) / 10$
= ₹ 5000

If face value is ₹. 5000, then investment $=₹ .7500$
and if face value is ₹. 100 then market value of each share $=(7500 \times 100)$ / 5000
= ₹ 150
19. A man buys 400 ten-rupee shares at a premium of $₹ .2 .50$ on each share. If the rate of dividend is $8 \%$, Find,
(i) his investment
(ii) dividend received
(iii) yield.

## Solution:

Given No. of shares $=400$
Face value of each share $=₹ 10$
Market value of each share
= ₹. 10 + ₹. 2.50
= ₹. 12.50
Rate of dividend $=8 \%$
Therefore, face value of 400 shares $=10 \times 400$
= ₹ 4000
(i) Total investment $=12.50 \times 400$
= ₹ 5000
(ii) Total dividend $=4000$
x (8/100)
= ₹ 320
(iii) Yield percent $=(320 \times 100) / 5000$
$=32 / 5$
$=6.4 \%$

20. A man invests ₹. 10400 in $6 \%$ shares at ₹. 104 and ₹. 11440 in 10.4\% shares at ₹. 143. How much income would he get in all ?

## Solution:

Given In fizt case; Total investment = ₹. 10400
Rate of dividend $=6 \%$
Market value of each share $=₹$. 104
Total dividend $=(10400 \times 6) / 104$
= ₹ 600
In second case, investment $=₹ 11440$
Rate of dividend $=10.4 \%$
Market value of each share $=₹ 143$
Therefore, total dividend $=(11440 \times 10.4) / 143$
= ₹ 832
Total dividend from both cases $=₹ .600+₹ .832$
= ₹. 1432
21. Two companies have shares of $7 \%$ at ₹. 116 and $9 \%$ at ₹. 145 respectively. In which of the shares would the investment be more profitable?

## Solution:

Let the investment in each case $=$ ₹. $116 \times 145$
Dividend in fǐt case,
$=(116 \times 145 \times 7) / 116$
= ₹ 1015
Dividend in second case
$=(116 \times 145 \times 9) / 145$
= ₹ 1044
From the above it is clear that the second type of shares that is $9 \%$ at ₹ 145 are more profitable.
22. Which is better investment : $6 \%$ ₹. 100 shares at ₹. 120 or $8 \%$ ₹. 10 shares at ₹. 15

## Solution:

Let the investment in each case $=₹ 120$ In the fist case,
Dividend on ₹. $120=$ ₹. 6
In second case, Dividend on ₹. 10
$=(8 \times 10) / 100$
$=0.8$
Now dividend on ₹ $15=0.8$
Then dividend on ₹ $120=(0.8 \times 120) / 15$
$=$ ₹ 6.4
From the above it is clear that the second type of shares that is $8 \%$ at ₹ 10 shares at 15 is more profitable.
23. A man invests ₹ 10080 in $6 \%$ hundred- rupee shares at ₹. 112. Find his annual income. When the shares fall to ₹. 96 he sells out the shares and invests the proceeds in $10 \%$ ten-rupee shares at ₹. 8 . Find the change in his annual income.

## Solution:

Given Investment = ₹. 10080
Face value of each share $=₹ 100$
Market value of each share $=₹ 112$
Rate of dividend $=6 \%$
Total income for the year
$=(10080 \times 6) / 112$
= ₹ 540
Number of shares $=10080 / 112$
$=90$
Selling price of 90 shares at the rate of ₹ 96 each $=90 \times 96$
= ₹ 8640
Rate of dividend in new shares $=10 \%$

Face value of each share $=₹ 10$
Market value of each share $=₹ 8$
Number of shares $=8640 / 8=1080$
Face value of 1080 shares $=1080 \times 10$
= ₹ 10800
Dividend $=(10800 \times 10) / 100$
= ₹ 1080
Difference in income $=1080-540$
$=₹ 540$ more
24. Sachin invests $\square 8500$ in $10 \% \square 100$ shares at $\square 170$. He sells the shares when the price of each share rises by $\square 30$. He invests the proceeds in $12 \% \square$ 100 shares at $\square 125$. Find
(i) the sale proceeds.
(ii) the number of $\square 125$ shares he buys.
(iii) the change in his annual income.

## Solution:

Given,
Investment $=\square 8500$
Face value of each share $=\square 100$
Market value of each share $=\square 170$
Rate of dividend $=10 \%$
Total income for the year
$=\square(8500 \times 10) / 170$
$=\square 500$
And, the number of shares $=8500 / 170=50$
Selling price of 50 shares at the rate of $\square(170+30)$ each $=\square 50 \times 200$
$=\square 10000$
(i) The sale proceeds $=\square 10000$

Rate of dividend in new shares $=12 \%$

Face value of each share = ₹ 100
Market value of each share $=₹ 125$
(ii) Number of shares $=10000 / 125=80$

Face value of 80 shares $=\square 80 \times 100$
= 8000
Dividend $=\square(8000 \times 12) / 100$
= 960
(iii) Hence, the change in his annual income $=\square(960-500)$
= 460 more
25. A pe₹on invests ₹. 4368 and buys certain hundred-rupee shares at 91 . He sells out shares worth ₹. 2400 when they have $t$ risen to 95 and the remainder when they have fallen to 85 . Find the gain or loss on the total transaction.

## Solution:

Given Investment = ₹. 4368
Market value of each share $=₹ .91$
Face value of each share $=$ ₹ 100
Therefore, number of shares $=4368 / 91$
$=48$
Face value of 24 shares $=24 \times 100$
= ₹ 2400
Sale price of shares worth ₹ $2400=(2400 \times 95) / 100$
= ₹ 2280
Face value of remaining shares $=24 \times 100$
= ₹ 2400
Sale price of shares of remaining amount $=(2400 \times 85) / 100$
= ₹ 2040
Total amount received $=2280+2040$
= ₹ 4320
Loss $=4368-4320$
= ₹ 48
26. By purchasing ₹. 50 gas shares for ₹. 80 each, a man gets $4 \%$ profit on his investment. What rate percent is company paying? What is his dividend if he buys 200 shares?

## Solution:

Given market value of each share $=₹ 80$
Face value of each share $=₹ 50$
Interest on investment $=4 \%$
Dividend on ₹ $80=(80 \times 4) / 100$
= 32/10
Percent dividend $=(32 / 10) \times(100 / 50)$
= 64/10
$=6.4 \%$
Number of shares $=200$
Face value of 200 shares $=200 \times 50$
= ₹ 10000
Dividend $=$ ₹ $10000 \times(6.4 / 100)$
= ₹ 640
27. ₹. 100 shares of a company are sold at a discount of ₹. 20. If the return on the investment is $15 \%$. Find the rate of dividend declared.

## Solution:

Market value of each shares $=100-20=₹ .80$
Interest on investment of ₹. $80=15 \% \times 80$
$=15 / 100$
$\times 80$
= ₹ 12
Dividend on face value of ₹. $100=₹ .12$
Rate of dividend $=12 \%$.
28. A company declared a dividend of $14 \%$. Find tire market value of ₹. 50 shares if the return on the investment was $10 \%$.

## Solution:

Rate of dividend $=14 \%$
Dividend on ₹. $50=(14 \times 50) / 100$
= ₹ 7
Now ₹. 10 is interest on the investment of $=₹ .100$
₹. 7 will be the interest on $=(100 \times 7) / 10=₹ .70$
Hence, market value of ₹. 50 shares $=₹ .70$
29. A company with 10000 shares of $₹ 100$ each, declares an annual dividend of $5 \%$.
(i) What is the total amount of dividend paid by the company ?
(ii) What would be the annual income of a man, who has 72 shares, in the company ?
(iii) If he received only $4 \%$ on his investment, find the price he paid for each share.

## Solution:

Given,
No. of shares $=10000$
Face value of each share $=$ ₹ 100
Rate of dividend $=5 \%$
(i) Total face value of 10000 shares
$=₹ 100 \times 10000$
= ₹. 1000000
Hence,
Total amount of dividend $=₹ .(1000000 \times 5) / 100$
= ₹. 50000
(ii) Income of 72 shares $=72 \times 5=₹ .360$
(iii) Rate of interest on investment $=4 \%$

Hence, market value of each share $=$ ₹. $100 / 4 \times 5$
= ₹. 125
30. A man sold some ₹. 100 shares paying $10 \%$ dividend at a discount of $25 \%$ and invested the proceeds in ₹. 100 shares paying $16 \%$ dividend quoted at ₹. 80 and thus increased his income by ₹. 2000. Find the number of shares sold by him.

## Solution:

Given,
Face value of each share = ₹. 100
Market value of each share $=₹ .100-₹ .25$
$=₹ 75$
Rate of dividend $=10 \%$
Let the no. of shares be taken as $x$
Selling price $=x \times 75=₹ .75 x$
Face value of x share $=100 \mathrm{x}$
Dividend annually $=100 x \times 10 / 100=10 x$
No. of shares purchased $=75 x / 80=15 x / 16$
Face value of $15 x / 16$ shares $=15 x / 16 \times 100=1500 x / 16$
Now, dividend $=1500 x / 16 \times 16 / 100=15 x$
Thus, the increase in the income $=15 x-10 x=5 x$
Now, we have
$5 x=2000$
$x=2000 / 5=400$
Hence, the number of shares purchased $=400$
31. A man invests ₹. 6750, partly in shares of $6 \%$ at ₹. 140 and partly in shares of $5 \%$ at ₹. 125. If his total income is ₹. 280 , how much has he invested in each ?

## Solution:

Let's consider the investment in fi₹t case to be $x$
Then, the investment in second case $=(6750-x)$

In fi₹t case, the dividend $=₹ . \times \times(6 / 140)$
$=$ ₹. $3 x / 70$
And dividend in second case $=₹ .(6750-x) \times(5 / 125)=₹ .(6750-x) / 25$
Total dividend $=3 x / 70+(6750-x) / 25$
Given that the total income = ₹. 280
So, we have
$3 x / 70+(6750-x) / 25=280$
$15 x+14(6750-x)=280 \times 350$ [Since, L.C.M $=350$ ]
$x=₹$. $[(280 \times 350)-(14 \times 6750)]$
$=₹$. $98000-94500$ )
$=₹ 3500$
Hence, investment in fi₹t case $=₹ 3500$
And investment in second case = ₹. 6750 - ₹. 3500
= ₹. 3250
32. Divide ₹. 20304 into two parts such that if one part is invested in 9\% ₹. 50 shares at 8\% premium and the other part is invested in 8\% ₹. 25 shares at 8\% discount, then the annual incomes from both the investment are equal.

## Solution:

Given,
Total amount = ₹ 20304
Let the amount invested in $9 \%$ ₹ 50 at $8 \%$ premium $=x$
Then, amount invested in 8\% ₹ 25 at $8 \%$ discount $=20304-x$
Income from both investments are equal Now income from fi₹t type of shares
$=(x \times 9) /(100+8)$
$=9 x / 108$
$=\mathrm{x} / 12$
Income from the second type of shares $=[(20304-x) \times 8] /(100-8)$
$=[(20304-x) \times 8] / 92$
$=2(20304-x) / 23$
As given, in both the cases the annual income is same, we have
$x / 12=2(20304-x) / 23$
$23 x=24(20304-x)$ [After cross multiplication]
$23 x=24 \times 20304-24 x$
$23 x+24 x=24 \times 20304$
$47 x=24 \times 20304$
$x=(24 \times 20304) / 47$
$=10368$
Hence, the amount invested in fizt kind of shares $=₹ 10368$
And in second kind of shares = ₹. 20304 - ₹. 10368
= ₹. 9936

## Chapter test

1. If a man received $\square 1080$ as dividend from $9 \% \square 20$ shares, find the number of shares purchased by him.

## Solution:

Income on one share $=9 / 100 \times 20$
= ₹ $9 / 5$
Therefore, no. of shares $=1080 \times 5 / 9$
$=120 \times 5$
$=600$
2. Find the percentage interest on capital invested in $18 \%$ shares when a ₹ 10 share costs ₹ 12.

## Solution:

Dividend on one share $=18 \%$ of ₹ 10
$=(18 \times 10) / 100$
$=$ ₹ $9 / 5$
Income on ₹ $12=9 / 5$

Then income of ₹ $100=(9 / 5) \times(100 / 12)$
$=15$
Percentage interest on capital $=15 \%$
3. Rohit Kulkami invests ₹ 10000 in $10 \%$ ₹ 100 shares of a company. If his annual dividend is ₹ 800, find :
(i) The market value of each share.
(ii) The rate percent which he earns on his investment.

## Solution:

Given investment = ₹ 10000
Face value of each share $=₹ 100$
Rate of dividend $=10 \%$
Annual dividend $=₹ 800$
(i) Market value $=(10000 \times 10) / 800$
= ₹ 125
(ii) rate percent on investment $=(800 \times 100) / 10000$
= 8\%
4. At what price should a $9 \%$ ₹ 100 share be quoted when the money is worth 6\% ?

Solution:
If interest is 6 then investment $=₹ 100$
and if interest is 9 , then investment
$=₹(100 \times 9) / 6$
= ₹ 150
Market value of each share $=₹ 150$
5. By selling at ₹ 92 , some $2.5 \%$ ₹ 100 shares and investing the proceeds in $5 \%$ ₹ 100 shares at ₹ 115 , a pe₹on increased his annual income by ₹ 90 . Find:
(i) the number of shares sold.
(ii) the number of shares purchased.
(iii) the new income.
(iv) the rate percent which he earns on his investment.

## Solution:

Given rate of dividend $=2.5 \%$
And market price = ₹ 92
Let number of shares purchased $=x$
Selling price of x shares $=92 \mathrm{x}$
Income from investing
₹ $\mathrm{x}=(92 \mathrm{x} \times 2.5) / 92$
$=(92 \times \times 25) /(92 \times 10)=(5 / 2) \times$
Again by investing $92 x$ in $5 \%$ at ₹ 115 the dividend $=(92 x \times 5) / 115=4 x$
Difference $=4 x-(5 / 2) x=3 / 2 x$
$3 / 2 x=90$
$x=(90 \times 2) / 3$
$=60$
(i) therefore, number of shares $=60$
(ii) Number of shares sold $=92 x / 115$
$=(92 \times 60) / 115$
$=48$
(iii) New income $=4 \mathrm{x}=4 \times 60$
= ₹ 240
(iv) Rate percent interest on investment $=(5 \times 100) / 115$
$=100 / 23$
= 4 ( $8 / 23$ )\%
6. A man has some shares of ₹. 100 par value paying $6 \%$ dividend. He sells half of these at a discount of $10 \%$ and invests the proceeds in $7 \%$ ₹. 50 shares at a premium of $₹$. 10 . This transaction decreases his income from dividends by ₹. 120. Calculate:
(i) the number of shares before the transaction.
(ii) the number of shares he sold.
(iii) his initial annual income from shares.

## Solution:

Let's consider the no. of shares to be $x$
Value of $x$ shares $=x \times 100=100 x$
And dividend $=(100 x \times 6) / 100=₹ .6 x$
Dividend on half-shares = ₹. $6 x / 2=₹ .3 x$
Now, the no. shares he sold out $=x / 2$
Amount received at $10 \%$ discount $=x / 2 \times 90=₹ .45 x$
In investing ₹. $45 x$, no. of shares he purchased $=45 x / 60$
Thus, the amount of shares $=45 x / 60 \times 50=₹ .225 x / 6$
Income at rate of $7 \%=255 x / 6 \times 7 / 100=21 x / 8$
Difference in income $=3 x-21 x / 8=3 x / 8$
According to the given conditions, we have
$3 x / 8=120$
$x=(120 \times 8) / 3$
$x=320$
Hence,
(i) The number of shares he hold initially $=320$
(ii) No. of shares he held later $=320 / 2=160$
(iii) Amount of income initially $=320 \times 6=₹ 1920$
7. Divide ₹. 101520 into two parts such that if one part is invested in $8 \%$ ₹. 100 shares at 8\% discount and the other in $9 \%$ ₹. 50 shares at $8 \%$ premium, the annual incomes are equal.

## Solution:

Given,
Total investment $=₹ 101520$
Let investment in fi₹t part be $x$ and in second part will be (101520-x)
Market value of fi₹t kind of shares = ₹. 100 - ₹. 8
= ₹. 92
And rate of dividend $=8 \%$

So, dividend $=(x \times 8) / 92=$ ₹. $2 x / 23$
Now, market value of second kind $=(101520-x)$
Rate of dividend $=9 \%$
And market value $=₹ .(100+8) / 100 \times 50$
$=₹$. $(108 / 100) \times 50$
$=₹ .54$
So, dividend $=₹ .(101520-x) \times 9 /(2 \times 54)$
$=₹ .(101520-x) / 12$
According to the given in the problem, we have

$$
\begin{aligned}
& 2 x / 23=(101520-x) / 12 \\
& 24 x=23(101520-x) \\
& 24 x=101520 \times 23-23 x \\
& 47 x=101520 \times 23 \\
& x=₹ .(101520 \times 23) / 47 \\
& =₹ .49680
\end{aligned}
$$

Hence, investment of fi₹t part $=₹ .49680$
And in second part $=₹ .(101520-49680)=₹ .51840$
8. A man buys ₹. 40 shares of a company which pays $10 \%$ dividend. He buys the shares at such a price that his profit is $16 \%$ on his investment. At what price did he buy each share?

## Solution:

Given,
Face value of each share $=₹ .40$
Dividend $=10 \%$
Gain on investment $=10 \%$
So, the dividend on ₹. $40=(40 \times 10) / 100=₹ .4$
Now, ₹. 16 is interest on the market value $=₹ .100$
Hence,
Market value if interest is ₹. $4=(100 \times 4) / 16$
= ₹. 25
9. A pe₹on invested $20 \%, 30 \%$ and $25 \%$ of his savings in buying shares at par values of three different companies $A, B$ and $C$ which declare dividends of $10 \%, 12 \%$ and $15 \%$ respectively. If his total income on account of dividends be ₹. 4675, find his savings and the amount which he invested in buying shares of each company.

## Solution:

Given that,
Investment in 3 companies A, B and C are 20\%, 30\% and 25\%
Let the total investment be ₹. 100
So, the investment in company $A=₹ .20$
Rate of dividend $=10 \%$
Thus, dividend $=₹ .(20 \times 10) / 100=₹ .2$
Investment in company $B=₹ .30$
Rate of dividend $=12 \%$
Thus, dividend $=₹ .(30 \times 12) / 100=₹ .36 / 10=₹ 3.6$
And, investment in company $C=₹ 25$
Rate of dividend $=25 \%$
Thus, dividend $=₹ .(25 \times 15) / 100=₹ .375 / 100=₹ .3 .75$
Total dividend $=₹ .2+₹ .3 .60+₹ 3.75=₹ .9 .35$
If dividend is ₹ 9.35 , then total savings $=₹ .100$
Then, if dividend is ₹. 4675 the total savings
$=(4675 \times 100) / 9.35$
$=(4675 \times 100 \times 100) / 935$
$=₹ 50000$
Hence,
The amount of investment in shares of company $A=₹ .50000 \times(20 / 100)=₹$. 10000
The amount of investment in shares of company $B=₹ .50000 \times(30 / 100)=₹$. 15000

The amount of investment in shares of company $A=₹ .50000 \times(25 / 100)=₹$. 12500
10. Virat and Dhoni invest ; 36000 each in buying shares of two companies. Virat buys $15 \% ; 40$ shares at a discount of $20 \%$, while Dhoni buys ;75 shares at a premium of $20 \%$. If both receive equal dividends at the end of the year, find the rate percent of the dividend declared by Dhoni's company.

## Solution:

In the fizt case, we have
Investment made by Virat $=\square 36000$
And market value at a discount of $20 \%=\square 40 \times(80 / 100)=\square 32$
Thus, total face value $=\square(36000 \times 40) / 32=\square 45000$
Rate of dividend $=15 \%$
Thus, total dividend $=\square(45000 \times 15) / 100=\square 6750$
Now, in second case, we have
Investment = 36000
Dividend of Dhoni $=\square 6750$
Face value of each share $=\square 75$
And market value at premium of $20 \%=\square 75 \times(120 / 100)=\square 90$
Face value $=36000 \times(75 / 90)=30000$
Thus, rate of dividend $=(6750 \times 100) / 30000 \%$

$$
=45 / 2 \%=22.5 \%
$$

